

Analysis of left-censored multiplex immunoassay data: A unified approach

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Talk Outline

Multiplex Immunoassays

Problem statement

Bayesian hierarchical model

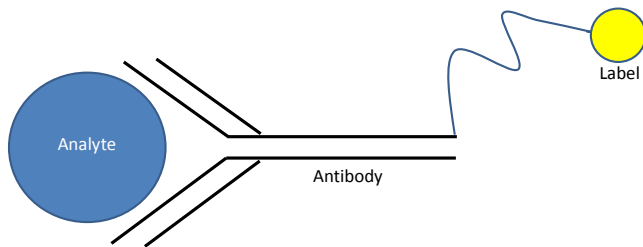
Simulation study

Application

Discussion

An immunoassay is ...

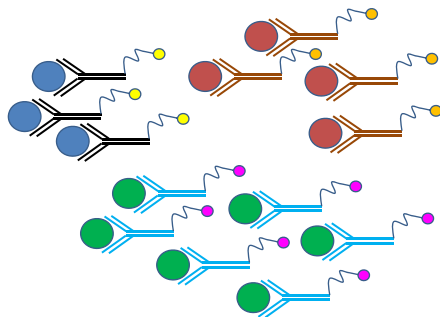
- A chemical test used to measure the concentration of a molecule in solution
- Target molecule - often a protein - called an *analyte*
- Analyte is “captured” by an analyte-specific antibody
- Measureable “label” (e.g. intensity of fluorescent signal) facilitates quantitation



Conventional uses

- Detect presence (absence) of a protein
 - Pregnancy test
 - Steroid use
 - Goal: *“Is analyte X detectable in this subject?”*
- Measure the concentration of protein
 - Blood panel
 - Viral load (HIV+ patients)
 - Goal: *“What is the concentration of analyte X for this subject?”*
- Emphasis is on **analyte measurement for an individual**

Multiplex immunoassay



- Simultaneous quantitation of a panel of analytes
- Commonly used as biomarker discovery tool
- Emphasis on **group-level comparisons**
- Goal
 - *“Is analyte X associated with disease status?”*
 - *“Does analyte X predict disease status?”*

Multiplex immunoassay

- All analytes accommodated on a single 96-well plate
- k -plex, $k = 5 - 30$ (typically)
- Multiple plates used to facilitate large sample sizes
- Each well detects all k analytes

	1	2	3	4	5	6	7	8	9	10	11	12
A	1	1	2	2	3	3	4	4	5	5	6	6
B		7	8	8	B	B	1	1	2	2	3	3
C	4	4	5	5	6	6	7	7	8	8	9	9
D	10	10	11	11	12	12	13	13	14	14	15	15
E	16	16	17	17	18	18	19	19	20	20	21	21
F	22	22	23	23	24	24	25	25	26	26	27	27
G	28	28	29	29	30	30	31	31	32	32	33	33
H	34	34	35	35	36	36	37	37	38	38	39	40

- Standards – serially diluted known analyte concentrations
- ◇ Blanks – no analyte concentration
- Patient samples – unknown analyte concentration

Workflow

For every analyte on each plate

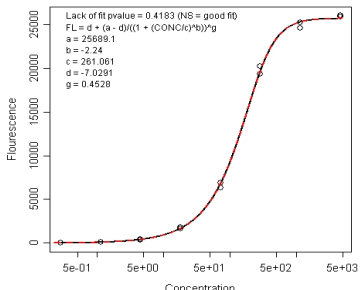
1. Place 8 – 10 duplicate standard concentrations
2. Place duplicate blanks
3. Use remaining wells for duplicate patient samples (serum, urine, saliva)
4. Measure signal intensity (*response*)
5. Calculate average response for blanks
6. “Correct” standard and patient responses by subtracting the average blank response
7. Fit a standard curve to paired known standard concentrations and background corrected (BgC) responses
8. Average the patient BgC responses
9. Back-fit average BgC patient response values to obtain estimates of analyte concentrations
10. Conduct group-level inference

Standard curve

5-Parameter Logistic Model

$$f(x_{ijk} | \beta_{jk}) = d_{jk} + \frac{a_{jk} - d_{jk}}{\left[1 + \left(\frac{x_{ijk}}{c_{jk}} \right)^{b_{jk}} \right]^{g_{jk}}}$$

where x_{ijk} is the i th known concentration for analyte j plate k and $\beta_{jk} = (a_{jk}, b_{jk}, c_{jk}, d_{jk}, g_{jk})'$.



a_{jk} - upper asymptote

d_{jk} - lower asymptote

b_{jk} - transition rate between asymptotes

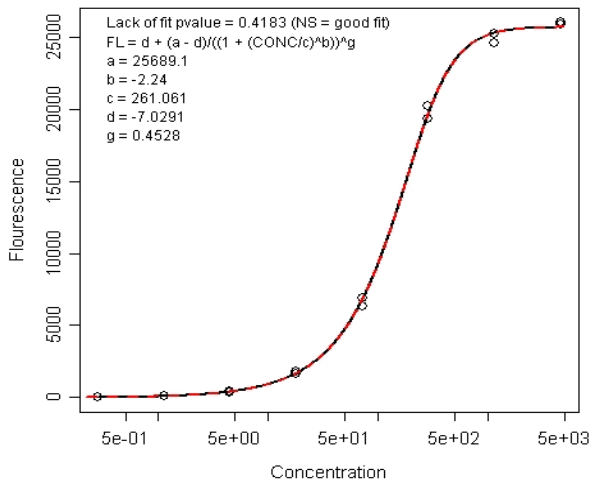
c_{jk} - concentration at inflection point

g_{jk} - asymmetry parameter

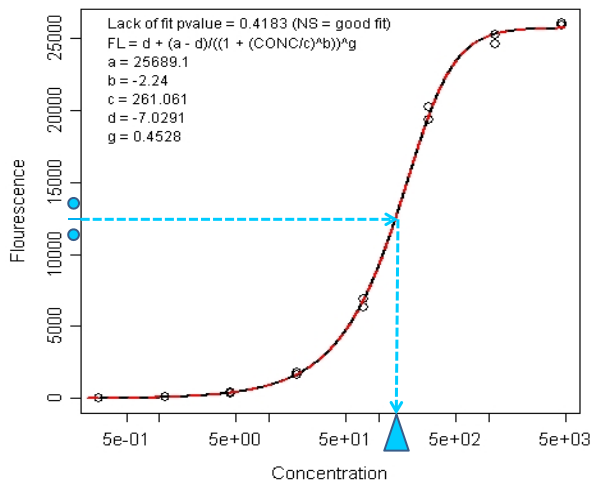
Fitting the 5-PL standard curve

- $y_{ijk\ell}^*$ = observed BgC response corresponding to ℓ th replicate of standard concentration x_{ijk}
- $y_{ijk\ell}^* \sim \text{Normal}(f(x_{ijk}|\beta_{jk}), \text{Var}(y_{ijk\ell}^*))$
- Variance systematically related to mean
 - Noise in signal detectors is proportional to response magnitude
 - Kinetics associated with antibody binding
 - Power of the mean variance function
 - $\text{Var}(y_{ijk\ell}^*) = \sigma_{jk}^2 f(x_{ijk}|\beta_{jk})^{2\theta}$
- Curve fitting achieved using generalized least squares (GLS)
- GLS = weighted least squares with weights estimated by $\text{Var}(y_{ijk\ell}^*)^{-1}$

Standard curve



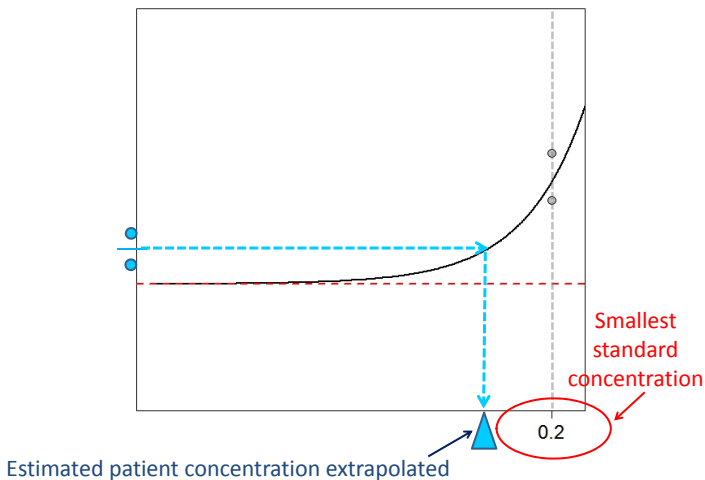
Patient analyte concentration estimation



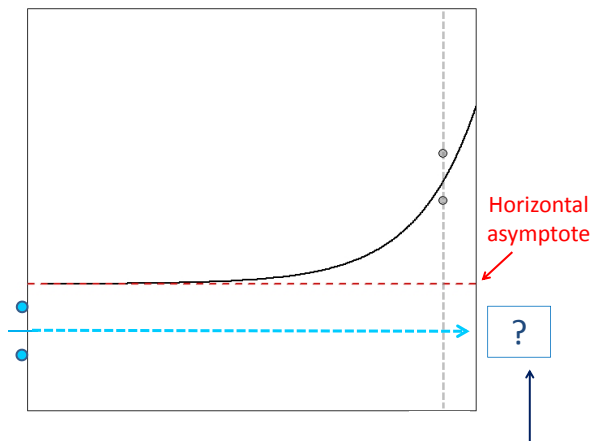
Sounds straightforward until you look at the data

Well	IL-1b	IL-2	IL-4	IL-5
B7,B8	*0.28	23.41	0.42	1.74
B9,B10	*0.61	51.61	1.07	3.94
B11,B12	OOB <	5.58	OOB <	OOB <
C1,C2	1.04	58.38	1.18	5.59
C3,C4	*0.79	63.17	1.66	5.69
C5,C6	*0.27	25.23	0.38	2.32
C7,C8	OOB <	8.46	OOB <	*0.45
C9,C10	*0.25	47.58	0.96	3.87
C11,C12	OOB <	OOB <	OOB <	OOB <
D1,D2	*0.19	27.14	0.52	2.17
D3,D4	OOB <	22.98	0.6	1.95
D5,D6	*0.48	46.6	0.95	4.44
D7,D8	10.07	8.21	OOB <	5.16
D9,D10	*0.71	50.53	1.24	3.8

Starred concentrations



OOR<



Back-fit fails – concentration can't be estimated

What causes this problem?

In biomarker discovery context

- Analytes' expected concentrations uncertain
- Results in poorly tuned dose-response curves
- Pervasive problem - percent of analytes with extrapolated or out-of-range concentrations can range from 0% - >90%
- Occurs less frequently at high end of curve

How can we analyze the data and address the investigator's research hypotheses?

Simple “solution”?

Well	IL-1b	IL-2	IL-4	IL-5
B7,B8	0	23.41	0.42	1.74
B9,B10	0	51.61	1.07	3.94
B11,B12	0	5.58	0	0
C1,C2	1.04	58.38	1.18	5.59
C3,C4	0	63.17	1.66	5.69
C5,C6	0	25.23	0.38	2.32
C7,C8	0	8.46	0	0
C9,C10	0	47.58	0.96	3.87
C11,C12	0	0	0	0
D1,D2	0	27.14	0.52	2.17
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Simple “solution”?

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B7,B8	0	23.41	0.42	1.74
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B11,B12	0	5.58	0	0
C1,C2	1.04	58.38	1.18	5.59
C3	<ul style="list-style-type: none">• Induces bias• Underestimates variability• Inflates type I error			
C5				
C7				
C9				
C1				
D1,D2	0	27.14	0.52	2.17
D3,D4	0	22.98	0.6	1.95
D5,D6	0	46.6	0.95	4.44
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D9,D10	0	50.53	1.24	3.8

Other ideas?

- Use established methods for analysis of left-censored data
 - ML with left-censored values contributing $1 - \text{CDF}$ to likelihood
 - Harrell's C-index - AUC equivalent for censored time-to-event data
- *Where to censor?*
- Conventional approach - censor at LOD or LOQ
- No established assay detection/quantitation limits
- Would need to be determined for each analyte and plate
- Previous efforts resulted in high rates of censored data - not an agreeable solution to the scientific investigator
- Shouldn't we account for uncertainty in curve and background estimation?

A “unified” approach

Incorporate **background** estimation, **standard curve** fitting, and **patient analyte concentration** estimation into a single Bayesian hierarchical model

1. *Background*

δ_{jk} = observed background for analyte j , plate k

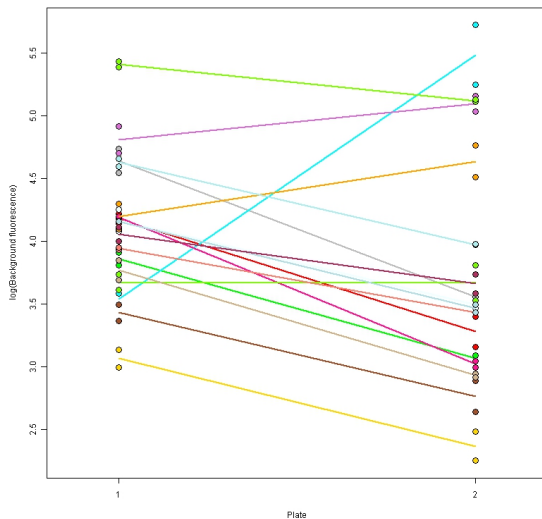
$$\log(\delta_{jk}) \sim \text{Normal}(\mu_{jk}, \varphi)$$

with

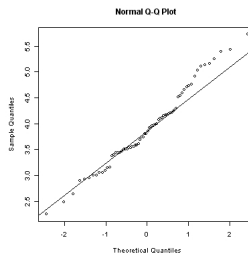
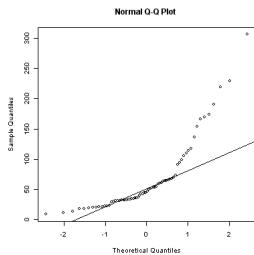
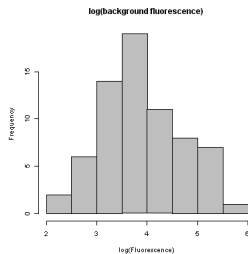
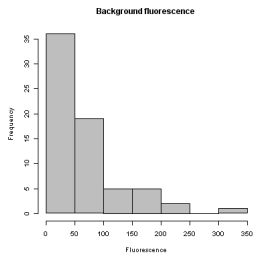
$$E(\delta_{jk}) = e^{\mu_{jk}}$$

$$\text{Var}(\delta_{jk}) = \lambda_{jk} = e^{2\mu_{jk}} e^{\varphi} (e^{\varphi} - 1)$$

Background mean



Background distribution



Standard curve

2. *Standard curve*

$y_{ijk\ell}$ = observed (not BgC) response corresponding to the ℓ th replicate of x_{ijk} , the i th known concentration for analyte j , plate k

$$y_{ijk\ell} | \mu_{jk} \sim \text{Normal}(f(x_{ijk} | \beta_{jk}) + e^{\mu_{jk}}, \tau_{ijk})$$

where

$$\tau_{ijk} = \sigma_{jk}^2 f(x_{ijk} | \beta_{jk})^{2\theta}$$

Patient data

3. *Patient analyte concentrations*

ν_{hj} = patient h 's true (latent) concentration of analyte j

$$\log(\nu_{hj}) \sim \text{Normal}(\gamma_{0j} + \gamma_{1j}D_h, \eta_j)$$

where

$$D_h = \begin{cases} 1, & \text{patient } h \text{ is disease positive} \\ 0, & \text{patient } h \text{ is disease negative.} \end{cases}$$

$e^{\gamma_{1j}}$ = fold-change comparing Ds+ to Ds- patients

Patient data

4. Patient response values

$z_{hjk\ell}$ = observed (not BgC) response corresponding to the ℓ th replicate of patient h 's true concentration for analyte j , plate k

$$z_{hjk\ell} | \mu_{jk} \sim \text{Normal}(f(\nu_{hj} | \beta_{jk}) + e^{\mu_{jk}}, \xi_{hjk})$$

where

$$\xi_{hjk} = \sigma_{jk}^2 f(\nu_{hj} | \beta_{jk})^{2\theta} \cdot \mathbf{1}(\nu_{hj} \geq x_{1hj}) + \lambda_{jk} \cdot \mathbf{1}(\nu_{hj} < x_{1hj})$$

Simulation study - experimental design

- Three plates
- Ten analytes per plate (“A” - “J”)
- Ten duplicate standards for each analyte
- Two blanks per plate
- Duplicate samples for 15 disease and 15 control subjects per plate (total sample size = 45 disease and 45 control)

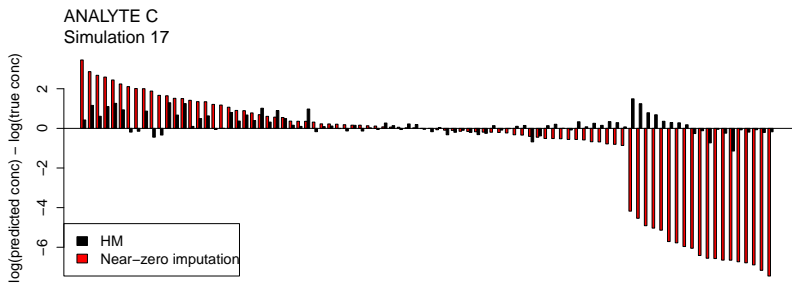
Simulation study - data description

- $\text{Prob}(\nu_{hj} < x_{1jk} | \text{control}) = 0.2 \forall j, k$
- $e^{\gamma_{ij}} = 1, 1.5, 2, 4,$ and 6 , respectively, for analytes A/F, B/G, C/H, D/I, and E/J
- For control subjects, $\text{SD}(\log \text{conc}) = 1$ for all analytes
- For disease subjects, $\text{SD}(\log \text{conc}) = 1$ for analytes A - E
- For disease subjects, $\text{SD}(\log \text{conc}) = 1.25$ for analytes F - J

Simulation study - inference

- 25 independent simulations in WinBUGS
- Burn-in = 50K iterations with posterior inference chain length of 10K
- Constructed FC and AUC from posterior estimates of patient analyte concentrations
- Compared to standard workflow
 - “Near-zero” imputation for low extrapolated or out-of-range concentrations
 - Linear regression for FC estimation and inference
 $H_0 : FC = 1$ vs $H_1 : FC \neq 1$
 - Empirical estimate of AUC with inference based on corresponding 95% CI
 $H_0 : AUC = 0.5$ vs $H_1 : AUC > 0.5$
- Type I error, power, coverage, bias, MSE to results using standard workflow

Results

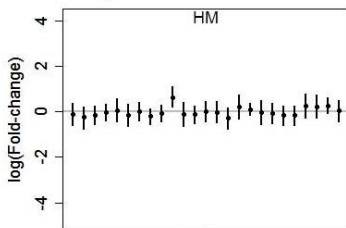


Fold change results

A: FC = 1.0

Prob(True Conc < Minimum Standard|Ctl) = 0.2

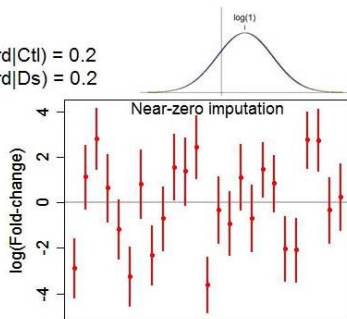
Prob(True Conc < Minimum Standard|Ds) = 0.2



Median bias = -0.031

Type I error rate = 1/25 = 0.04

Coverage = 24/25 = 0.96



Median bias = 0.297

Type I error rate = 12/25 = 0.48

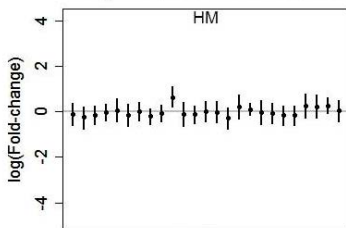
Coverage = 13/25 = 0.52

Fold change results

A: FC = 1.0

Prob(True Conc < Minimum Standard|Ctl) = 0.2

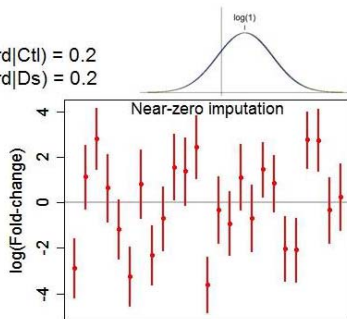
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Type I error rate = 12/25 = 0.48

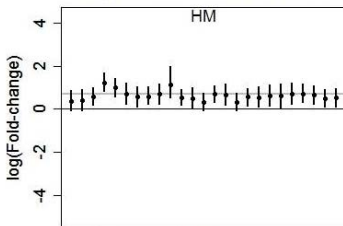
Coverage = 13/25 = 0.52

Fold change results

C: FC = 2

$\text{Prob}(\text{True Conc} < \text{Minimum Standard|Ctl}) = 0.2$

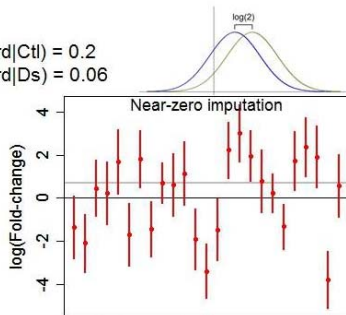
$\text{Prob}(\text{True Conc} < \text{Minimum Standard|Ds}) = 0.06$



Median bias = -0.215

Power = 21/25 = 0.84

Coverage = 24/25 = 0.96



Median bias = -0.248

Power = 16/25 = 0.64

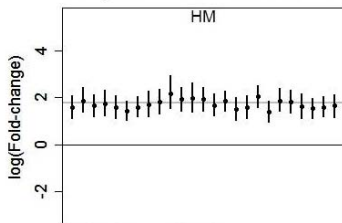
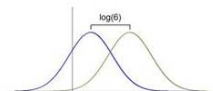
Coverage = 12/25 = 0.48

Fold change results

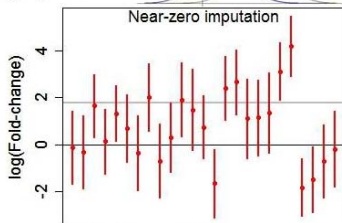
E: FC = 6

Prob(True Conc < Minimum Standard|Ctl) = 0.2

Prob(True Conc < Minimum Standard|Ds) = 0.004



Median bias = -0.693
Power = 25/25 = 1
Coverage = 25/25 = 1



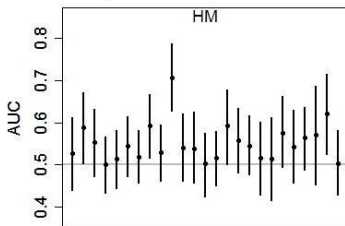
Median bias = -1.908
Power = 11/25 = 0.44
Coverage = 16/25 = 0.64

AUC results

A: AUC = 0.5

Prob(True Conc < Minimum Standard|Ctl) = 0.2

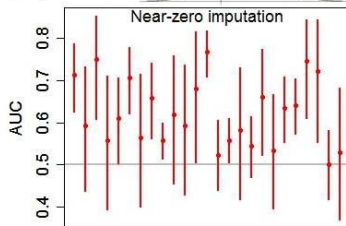
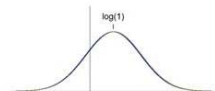
Prob(True Conc < Minimum Standard|Ds) = 0.2



Median bias = 0.043

Type I error rate = 5/25 = 0.2

Coverage = 20/25 = 0.8



Median bias = 0.109

Type I error rate = 14/25 = 0.56

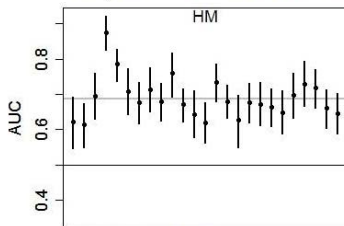
Coverage = 11/25 = 0.44

AUC results

C: AUC = 0.69

Prob(True Conc < Minimum Standard|Ct) = 0.2

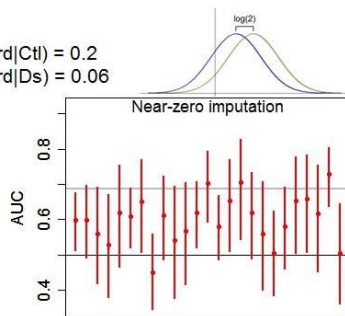
Prob(True Conc < Minimum Standard|Ds) = 0.06



Median bias = -0.011

Power = 25/25 = 1

Coverage = 20/25 = 0.8



Median bias = -0.080

Power = 10/25 = 0.4

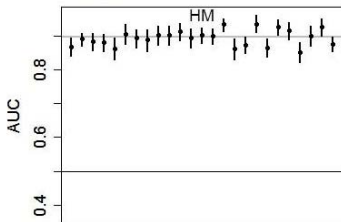
Coverage = 19/25 = 0.76

AUC results

E: AUC = 0.90

Prob(True Conc < Minimum Standard|Ctl) = 0.2

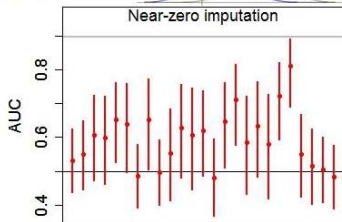
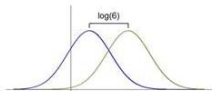
Prob(True Conc < Minimum Standard|Ds) = 0.004



Median bias = -0.002

Power = 25/25 = 1

Coverage = 15/25 = 0.6



Median bias = -0.299

Power = 6/25 = 0.24

Coverage = 0/25 = 0

Head and neck cancer application

Hypothesis: HPV16 infection affects tumor immunity, resulting in differences between patients with HPV-associated and non-associated head and neck cancer tumors.

- Serum samples from 15 HPV+, 18 HPV-, and 19 control patients
- Multiplex analysis of 9 cytokines and chemokines
- Two plates
- Eight standards per analyte and plate
- Two background wells per analyte per plate
- All patient samples measured in duplicate
- Percent of estimated concentrations below minimum standard (based on standard workflow) ranges from 0% to 41%
- FC and AUC estimated using hierarchical model

HNCA results

IL6 was 3.4-times higher in HPV- samples relative to control (FC = 3.4, 95% CI = 1.6 to 7.9).

Cytokines significantly predictive of HPV-associated and non-associated HNCA, based on AUC posterior inference. AUC (95% CI)			
Analyte	HPV-:Ctl	HPV-:HPV+	HPV+:Ctl
GCSF	0.70 (0.56, 0.83)	0.54 (0.39, 0.68)	0.66 (0.51, 0.79)
IL4	0.58 (0.49, 0.67)	0.64 (0.54, 0.73)	0.45 (0.33, 0.56)
IL6	0.79 (0.75, 0.83)	0.67 (0.63, 0.71)	0.65 (0.59, 0.70)
IL12	0.61 (0.54, 0.68)	0.60 (0.53, 0.69)	0.51 (0.41, 0.60)
MCP1	0.66 (0.61, 0.70)	0.59 (0.54, 0.64)	0.54 (0.48, 0.60)
MIP1b	0.52 (0.48, 0.56)	0.46 (0.42, 0.51)	0.55 (0.51, 0.60)
TNFa	0.62 (0.55, 0.68)	0.58 (0.50, 0.66)	0.55 (0.47, 0.62)

Summary

- What we've learned so far
 - If goal is biomarker discovery, near-zero imputation is a bad idea
 - FC estimation and inference has good accuracy
 - AUC estimation and inference seems slightly conservative
- What's left
 - Additional simulations
 - Compare to censored data approaches

Future directions

- Multivariate distribution for analyte concentrations
- Design considerations - number of background replicates, number of plates (sample size)
- Flexible dose-response curve fitting - e.g. splines
- Hopefully the next grant!

Acknowledgements

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Thank you!