

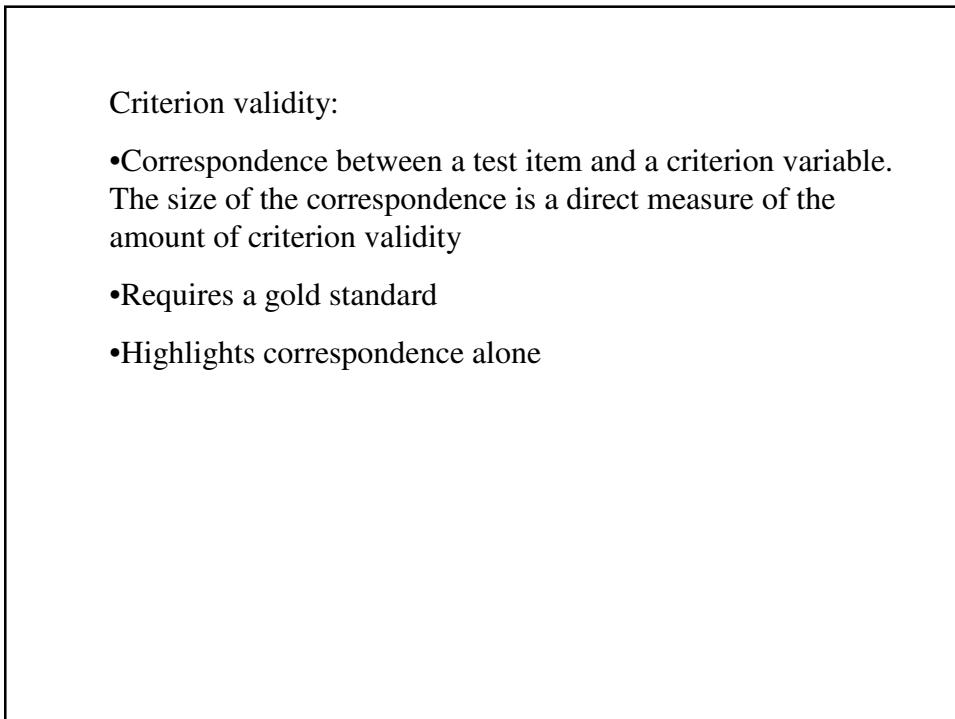
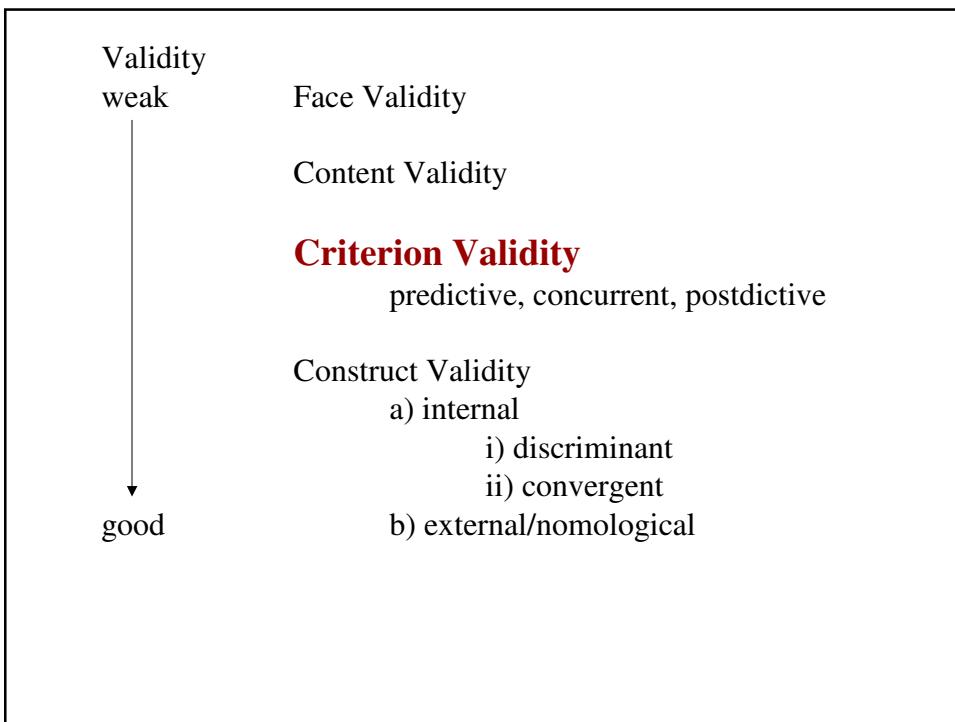
# Validity II

Session 08, Lecture 06

9/20/06

## Outline

- Roadmap
- Criterion Validity – ROC
- Construct Validity - MTMC



## Sensitivity & Specificity

		Disease Status		
		Yes (D+)	No (D-)	
Test Result	T+	A	B	$\Pr(T+) = A+B/N$
	T-	C	D	$\Pr(T-) = C+D/N$
		$\Pr(D+) = A+C/N$	$\Pr(D-) = B+D/N$	N

- Sensitivity – Does the Test Identify Cases?

$$P(T+|D+) = \frac{A}{A+C}$$

- Specificity – Does the test Identify Non-cases?

$$P(T-|D-) = \frac{D}{B+D}$$

## Positive & Negative Predictive Value

		Disease Status		
		Yes (D+)	No (D-)	
Test Result	T+	A	B	$\Pr(T+) = A+B/N$
	T-	C	D	$\Pr(T-) = C+D/N$
		$\Pr(D+) = A+C/N$	$\Pr(D-) = B+D/N$	N

- PPV – What does a positive test result mean?

$$P(D+|T+) = \frac{A}{A+B}$$

- Specificity – What does a negative test result mean?

$$P(D-|T-) = \frac{D}{C+D}$$

Sensitivity and Specificity of a Blood Glucose Level of 5.6 mM for Determination of Diabetes Status

— True Disease Status —

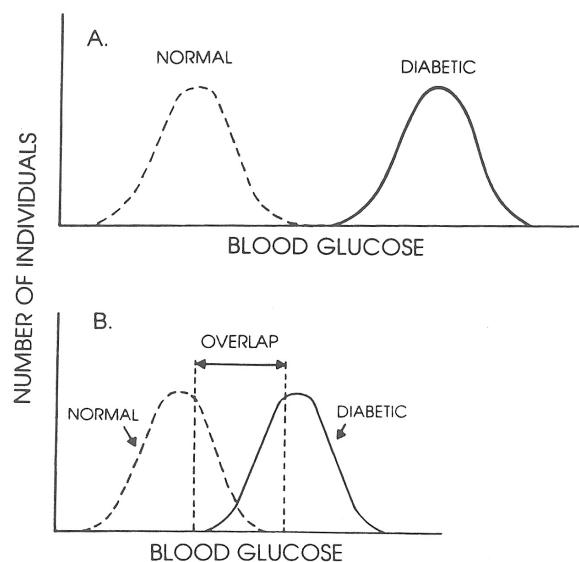
Blood Glucose Level (mM)	Diabetics	Nondiabetics
$\geq 5.6$ mM classified as diabetics	62 (A)	215 (B)
<5.6 mM classified as nondiabetics	1 (C)	125 (D)

Sensitivity =

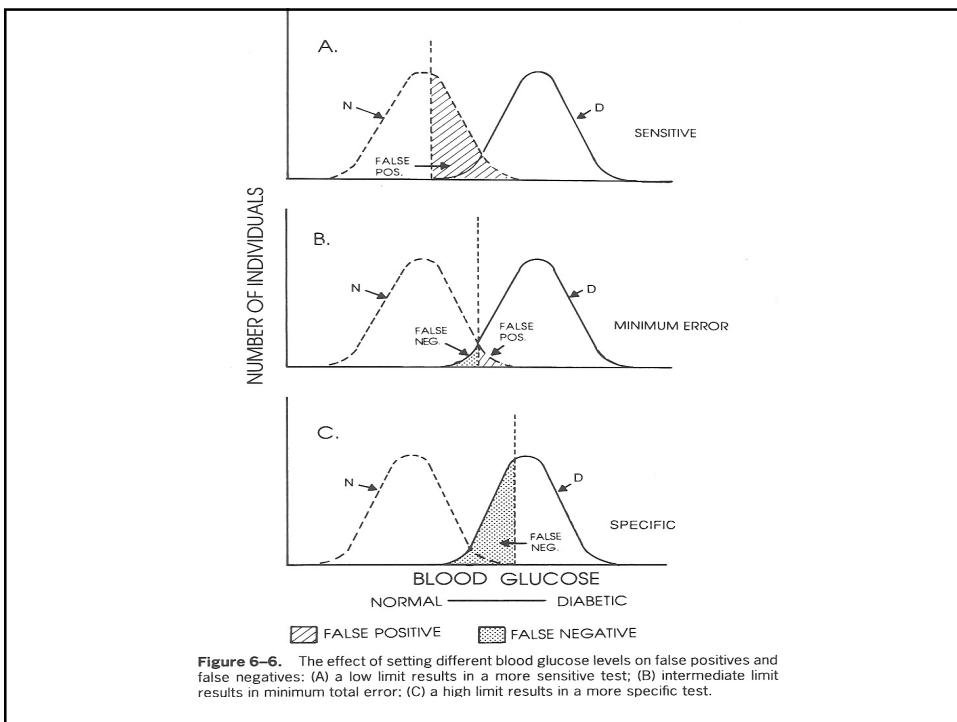
Specificity =

Positive predictive value =

Negative predictive value =



**Figure 6–5.** Hypothetical distribution of blood glucose values in (A) normal and diabetic population without any overlap and in (B) normal and diabetic populations with overlapping values.



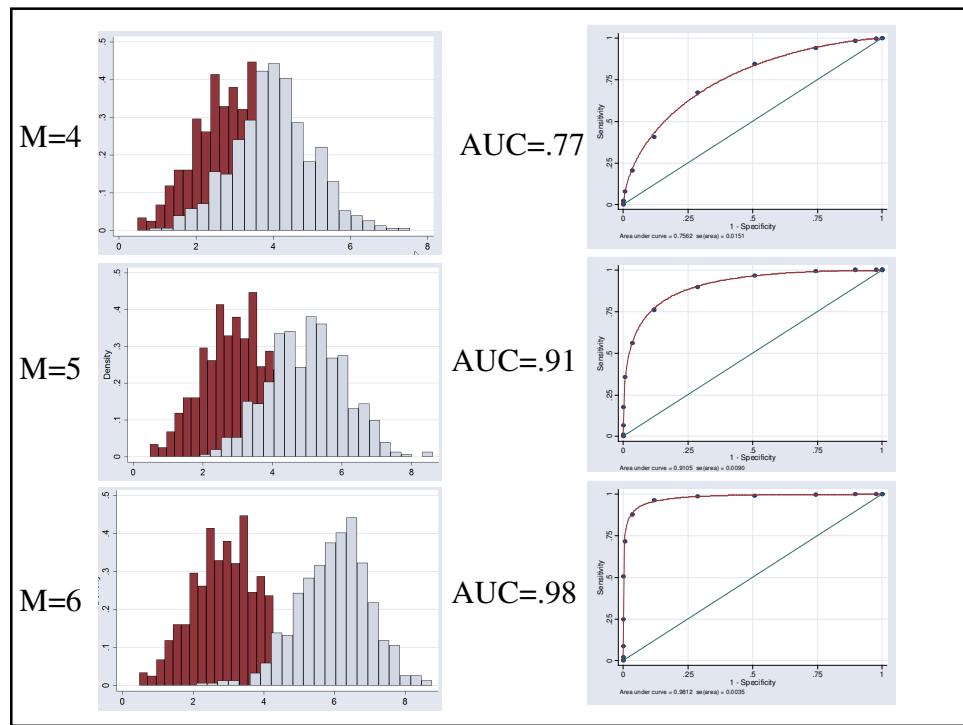
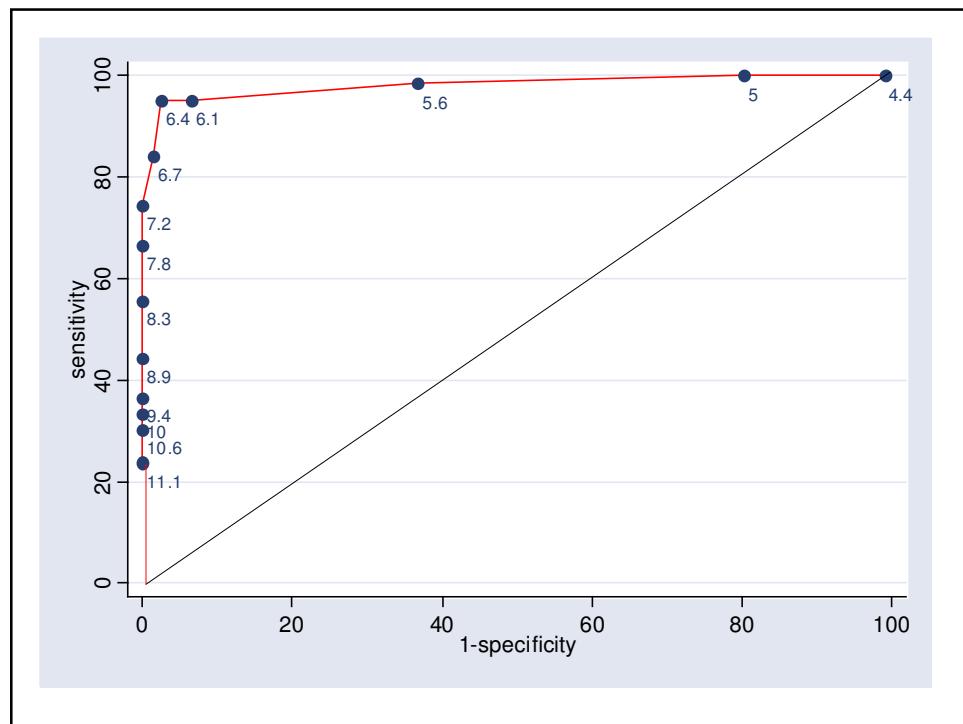
**Figure 6-6.** The effect of setting different blood glucose levels on false positives and false negatives: (A) a low limit results in a more sensitive test; (B) intermediate limit results in minimum total error; (C) a high limit results in a more specific test.

**Table 6-9.** Sensitivity and Specificity of a Two-Hour Postprandial Blood Test for Glucose for 63 True Diabetics and 340 True Nondiabetics at Different Levels of Blood Glucose

REFERENCE VALUE (mg/dl)	BLOOD GLUCOSE (mM)	SENSITIVITY <sup>1</sup> (%)	SPECIFICITY <sup>1</sup> (%)
80	4.4	100.0 (63/63)	0.6 ( 2/340)
	5.0	100.0 (63/63)	19.7 ( 67/340)
	5.6	98.4 (62/63)	63.2 (215/340)
	6.1	95.2 (60/63)	93.5 (318/340)
115	6.4	95.2 (60/63)	97.4 (331/340)
	6.7	84.1 (53/63)	100.0 (335/340)
	7.2	74.6 (47/63)	100.0 (340/340)
140	7.8	66.7 (42/63)	100.0 (340/340)
	8.3	55.6 (35/63)	100.0 (340/340)
	8.9	44.4 (28/63)	100.0 (340/340)
	9.4	36.5 (23/63)	100.0 (340/340)
	10.0	33.3 (21/63)	100.0 (340/340)
	10.6	30.2 (19/63)	100.0 (340/340)
200	11.1	23.8 (15/63)	100.0 (340/340)

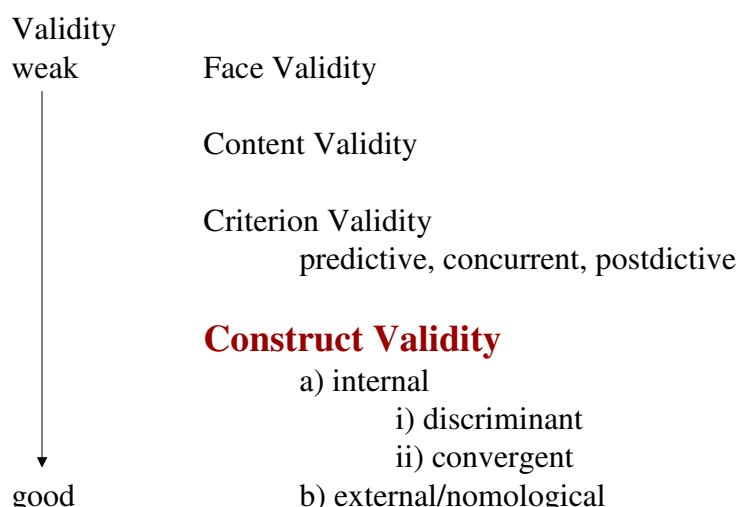
Figures in parentheses are the number of diabetics with a two-hour postprandial blood glucose level at or above the specified level.

Source: Wadena City Health Study (unpublished).



Relation between the Prevalence of Disease in a Population and the Positive and Negative Predictive Value of a Test

Population Prevalence Rate (per 100 persons)	Sensitivity	Specificity	Positive Predictive Value	Negative Predictive Value
15.6	.98	.37	.22	.99
23	.98	.37	.32	.99
37.5	.98	.37	.48	.97



## Multi-trait Multi-method

- Assesses construct validity
- Campbell & Fiske (1959)
- multiple concepts (traits) and multiple methods (scales or observers)
- matrix of correlation coefficients

## Synthetic Example- Method Blocks

		method 1			method 2			method 3		
		A	B	C	A	B	C	A	B	C
traits	method 1	A	B	C	mono method					
	method 2	A	B	C	hetero method		mono method			
	method 3	A	B	C	hetero method		hetero method		mono method	

## Synthetic Example – Reliability Diagonals

Reliability Coefficients should be the highest values in the matrix

		method 1			method 2			method 3			
		traits	A	B	C	A	B	C	A	B	C
method	method	A	(.89)								
		B		(.89)							
		C			(.76)						
method	method	A				(.93)					
		B					(.94)				
		C						(.84)			
method	method	A							(.94)		
		B							(.92)		
		C								(.85)	

## Synthetic Example – Validity Diagonals

Validity coefficients (Mono-trait Hetero-method – MTHM)  
these should be sig. different from 0 (convergent)

		method 1			method 2			method 3			
		traits	A	B	C	A	B	C	A	B	C
method	method	A	(.89)								
		B		(.89)							
		C			(.76)						
method	method	A	.57			(.93)					
		B		.57			(.94)				
		C			.46			(.84)			
method	method	A	.56			.67			(.94)		
		B		.58			.66			(.92)	
		C			.45			.58			(.85)

## Synthetic Example – Hetero-trait Mono-method

Validity coefficients should be greater than any HTMM coefficients (traits should “hang together” more closely than methods)

		method 1			method 2			method 3			
		traits	A	B	C	A	B	C	A	B	C
method 1	A	(.89)									
	B	.51	(.89)								
	C	.38	.37	(.76)							
method 2	A	.57				(.93)					
	B		.57			.68	(.94)				
	C			.46		.59	.58	(.84)			
method 3	A	.56				.67			(.94)		
	B		.58				.66		.67	(.92)	
	C			.45				.58	.58	.60	(.85)

## Synthetic MTMM – Hetero-trait Heter-method

Validity coefficients should be greater than the HTHM coefficients in the same row and column

		method 1			method 2			method 3			
		traits	A	B	C	A	B	C	A	B	C
method 1	A	(.89)									
	B		(.89)								
	C			(.76)							
method 2	A	.57	.22	.09		(.93)					
	B	.22	.57	.10			(.94)				
	C	.11	.11	.46				(.84)			
method 3	A	.56	.22	.11		.67	.42	.33	(.94)		
	B	.23	.58	.12		.43	.66	.34		(.92)	
	C	.11	.11	.45		.34	.32	.58			(.85)

MTMM(Reliability) >
 MTHM(Validity) >
 HTHM  
HTHM

		method 1			method 2			method 3		
		A	B	C	A	B	C	A	B	C
traits	method 1	.89								
	method 2	.51	.89							
	method 3	.38	.37	.76						
methods	method 1	.57	.2	.09	.93					
	method 2	.22	.57	.10	.68	.94				
	method 3	.11	.11	.46	.59	.58	.84			
method 1	A	.56	.22	.11	.67	.42	.33	.94		
	B	.23	.58	.12	.43	.66	.34	.67	.92	
	C	.11	.11	.45	.34	.32	.58	.58	.60	.85

## Another Perspective (Inside out)...

		trait A			trait B			trait C		
		1	2	3	1	2	3	1	2	3
Trait A	method 1	.89								
	method 2	.57	.89							
	method 3	.56	.67	.76						
Trait B	method 1	.51	.2	.22	.93					
	method 2	.22	.68	.42	.57	.94				
	method 3	.23	.43	.67	.58	.66	.84			
Trait C	method 1	.38	.09	.11	.37	.10	.12	.94		
	method 2	.11	.59	.33	.11	.58	.34	.46	.92	
	method 3	.11	.34	.58	.11	.32	.60	.45	.58	.85

A Multitrait-Multimethod Matrix Assessing Children's Mental Disorders									
	<i>Child</i>			<i>Mother</i>			<i>Father</i>		
	Dep.	Anx.	Ext.	Dep.	Anx.	Ext.	Dep.	Anx.	Ext.
<i>Child</i>									
Dep.	.75								
Anx.		.74							
Ext.			.72						
<i>Mother</i>									
Dep.	.26			.71					
Anx.		.22			.76				
Ext.			.41			.81			
<i>Father</i>									
Dep.	.11			.27			.65		
Anx.		.05			.48			.62	
Ext.			.21			.57			.76

A Multitrait-Multimethod Matrix Assessing Children's Mental Disorders									
	<i>Child</i>			<i>Mother</i>			<i>Father</i>		
	Dep.	Anx.	Ext.	Dep.	Anx.	Ext.	Dep.	Anx.	Ext.
<i>Child</i>									
Dep.	.75								
Anx.		.74							
Ext.			.72						
<i>Mother</i>									
Dep.	.26	.24	.15	.71					
Anx.	.15	.22	-.00		.76				
Ext.	.38	.34	.41			.81			
<i>Father</i>									
Dep.	.11	.10	.07	.27	.21	-.04	.65		
Anx.	-.01	.05	-.12	.31	.48	.10		.62	
Ext.	.24	.19	.21	.21	.16	.57			.76

A Multitrait-Multimethod Matrix Assessing Children's Mental Disorders									
	Child			Mother			Father		
	Dep.	Anx.	Ext.	Dep.	Anx.	Ext.	Dep.	Anx.	Ext.
<i>Child</i>									
Dep.	.75								
Anx.	.38	.74							
Ext.	.51	.55	.72						
<i>Mother</i>									
Dep.	.26	.24	.15	.71					
Anx.	.15	.22	-.00	.64	.76				
Ext.	.38	.34	.41	.35	.31	.81			
<i>Father</i>									
Dep.	.11	.10	.07	.27	.21	-.04	.65		
Anx.	-.01	.05	-.12	.31	.48	.10	.48	.62	
Ext.	.24	.19	.21	.21	.16	.57	.30	.29	.76

A Multitrait-Multimethod Matrix Assessing Children's Mental Disorders						
Mental Disorder	Ci	Ce	Mi	Me	Fi	Fe
<i>Child Report</i>						
Internalizing		.77				
Externalizing	.64	.74				
<i>Mother Report</i>						
Internalizing	.28	.07	.78			
Externalizing	.43	.41	.36	.81		
<i>Father Report</i>						
Internalizing	.09	-.03	.42	.04	.68	
Externalizing	.26	.21	.21	.57	.34	.76